

# Vibration localization in weakly coupled airfoils subjected to flutter instability

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**Abstract.** Very commonly, engineering structures are constituted by unit cells assembled in an axisymmetric fashion. Examples are blisks, turbine and compressor rotors, wind turbines, space antennas and reflectors. Here, a homogeneous cyclic symmetric nonlinear lumped structure constituted by  $N$  elastically coupled airfoils invested by a uniform airstream and subjected to flutter instability is studied. Due to the system's nonlinearities, multiple stable spatially localized vibrating states are found. First numerical results are shown, then a minimal model of weakly coupled nonlinear beams is tested experimentally to prove that nonlinear localization may take place in engineering relevant structures.

## Introduction

Several engineering structures are constituted by mechanical components assembled in a nearly cyclic and symmetric structure, such as aeroengine turbo fan, turbine rotors and space structures. The repeating unit cell is often constituted by a slender beam (e.g. the blade in a wind turbine), which is jointed to a hub providing the weak elastic coupling between neighbour unit cells. It is known since the 50's, that small disorder in linear mechanical systems could lead to spatial localization of vibration [1], known in turbomachinery as "mistuning". Later studies have shown that vibration localization may take place also in perfectly homogeneous but nonlinear systems [2-3]. A key characteristic of these systems is that the unit cell has multiple co-existing stable solutions (fixed points and/or limit cycles) in certain range of the governing parameters. Here, the case of a homogeneous cyclic symmetric nonlinear lumped structure constituted by  $N$  elastically coupled airfoils, with plunge "h" and pitch " $\alpha$ " degrees of freedom, invested by a uniform airstream at velocity  $V$  and subjected to flutter instability is studied.

## Results and Discussion

The aerodynamic lift and moment exerted on the thin airfoil (the unit cell, Fig. 1a) due to the uniform airstream, are obtained using the model by Fung [4]. By changing the cubic stiffness coefficient of the plunge, the HOPF bifurcation changes its character from super- to subcritical. In the subcritical setting there exists an interval of  $V$  for which the single airfoil shows multiple spatially localized vibrating states, which involve a fixed point, a limit cycle or irregular motion. This multiplicity of solutions give rise to coexisting spatially localized vibration patterns (Fig. 1b) when multiple elastically coupled airfoils are considered.

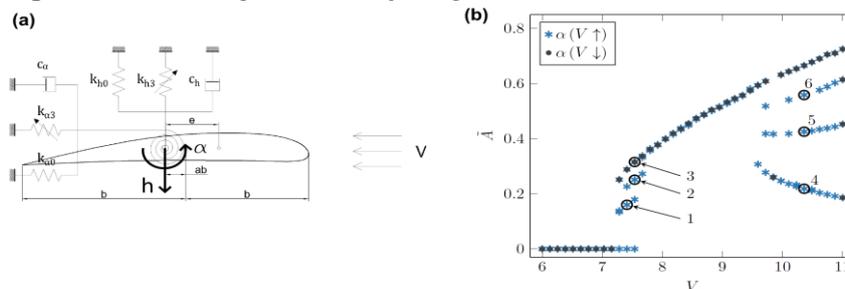


Figure 1: (a) sketch of the single airfoil with plunge "h" and pitch " $\alpha$ " degrees of freedom. (b) Vibration amplitude of the pitch degree of freedom as a function of the airstream velocity

Due to the multiplicity of coexisting stable solutions (Fig. 1b) the question of how likely the system converges to a certain state is addressed. A plausible set of initial conditions is selected and the concept of *basin stability* analysis is exploited to assess, for the structure of  $N$  coupled airfoils, the likelihood to converge to a certain state. Lastly, the measurements obtained with a test rig constituted by a chain of weakly coupled slender beams with clearance nonlinearities are shown to prove that the nonlinear localization of vibrations is possible for engineering relevant structures.

## References

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